



General Certificate of Education  
Advanced Level Examination  
January 2012

# Mathematics

# MM2B

## Unit Mechanics 2B

Wednesday 25 January 2012 1.30 pm to 3.00 pm

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.  
You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take  $g = 9.8 \text{ m s}^{-2}$ , unless stated otherwise.

**Information**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.

- 1** A plane is dropping packets of aid as it flies over a flooded village. The speed of a packet when it leaves the plane is  $60 \text{ m s}^{-1}$ . The packet has mass 25 kg.

The packet falls a vertical distance of 34 metres to reach the ground.

- (a) Calculate the kinetic energy of the packet when it leaves the plane. (2 marks)
- (b) Calculate the potential energy lost by the packet as it falls to the ground. (2 marks)
- (c) Assume that the effect of air resistance on the packet as it falls can be neglected.
- (i) Find the kinetic energy of the packet when it reaches the ground. (2 marks)
- (ii) Hence find the speed of the packet when it reaches the ground. (2 marks)
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- 2** A particle, of mass 50 kg, moves on a smooth horizontal plane. A single horizontal force

$$[(300t - 60t^2) \mathbf{i} + 100e^{-2t} \mathbf{j}] \text{ newtons}$$

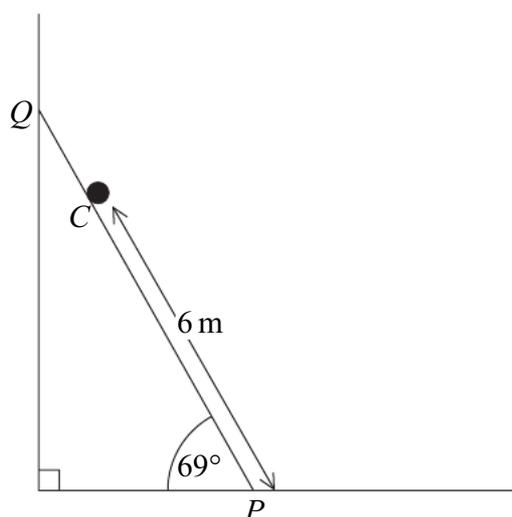
acts on the particle at time  $t$  seconds.

The vectors  $\mathbf{i}$  and  $\mathbf{j}$  are perpendicular unit vectors.

- (a) Find the acceleration of the particle at time  $t$ . (2 marks)
- (b) When  $t = 0$ , the velocity of the particle is  $(7\mathbf{i} - 4\mathbf{j}) \text{ m s}^{-1}$ .  
Find the velocity of the particle at time  $t$ . (4 marks)
- (c) Calculate the speed of the particle when  $t = 1$ . (4 marks)

- 3 A uniform ladder  $PQ$ , of length 8 metres and mass 28 kg, rests in equilibrium with its foot,  $P$ , on a rough horizontal floor and its top,  $Q$ , leaning against a smooth vertical wall. The vertical plane containing the ladder is perpendicular to the wall and the angle between the ladder and the floor is  $69^\circ$ .

A man, of mass 72 kg, is standing at the point  $C$  on the ladder so that the distance  $PC$  is 6 metres. The man may be modelled as a particle at  $C$ .

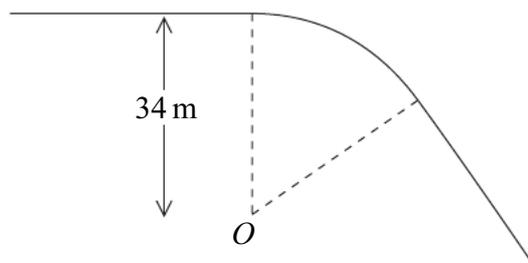


- (a) Draw a diagram to show the forces acting on the ladder. (2 marks)
- (b) With the man standing at the point  $C$ , the ladder is on the point of slipping.
- (i) Show that the magnitude of the reaction between the ladder and the vertical wall is 256 N, correct to three significant figures. (4 marks)
- (ii) Find the coefficient of friction between the ladder and the horizontal floor. (4 marks)
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- 4 A car travels along a straight horizontal road. When its speed is  $v\text{ m s}^{-1}$ , the car experiences a resistance force of magnitude  $25v$  newtons.
- (a) The car has a maximum constant speed of  $42\text{ m s}^{-1}$  on this road.
- Show that the power being used to propel the car at this speed is 44 100 watts. (2 marks)
- (b) The car has mass 1500 kg.
- Find the acceleration of the car when it is travelling at  $15\text{ m s}^{-1}$  on this road under a power of 44 100 watts. (4 marks)

Turn over ►

- 5 A parcel is placed on a flat rough horizontal surface in a van. The van is travelling along a horizontal road. It travels around a bend of radius 34 m at a constant speed. The coefficient of friction between the parcel and the horizontal surface in the van is 0.85.

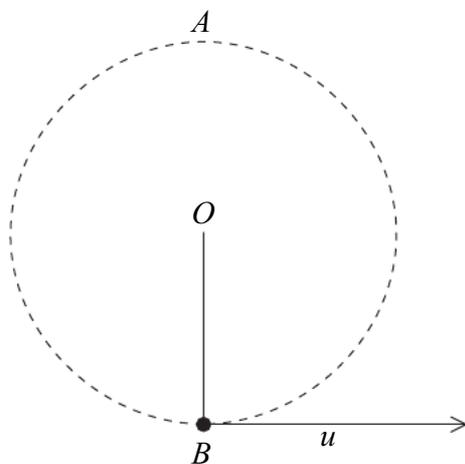
Model the parcel as a particle travelling around part of a circle of radius 34 m and centre  $O$ , as shown in the diagram.



Find the greatest speed at which the van can travel around the bend without causing the parcel to slide. (6 marks)

- 6 Alice places a toy, of mass 0.4 kg, on a slope. The toy is set in motion with an initial velocity of  $1 \text{ m s}^{-1}$  down the slope. The resultant force acting on the toy is  $(2 - 4v)$  newtons, where  $v \text{ m s}^{-1}$  is the toy's velocity at time  $t$  seconds after it is set in motion.
- (a) Show that  $\frac{dv}{dt} = -10(v - 0.5)$ . (2 marks)
- (b) By using  $\int \frac{1}{v - 0.5} dv = -\int 10 dt$ , find  $v$  in terms of  $t$ . (5 marks)
- (c) Find the time taken for the toy's velocity to reduce to  $0.55 \text{ m s}^{-1}$ . (3 marks)

- 7 A small bead, of mass  $m$ , is suspended from a fixed point  $O$  by a light inextensible string of length  $a$ . With the string taut, the bead is at the point  $B$ , vertically below  $O$ , when it is set into vertical circular motion with an initial horizontal velocity  $u$ , as shown in the diagram.



The string does not become slack in the subsequent motion. The velocity of the bead at the point  $A$ , where  $A$  is vertically above  $O$ , is  $v$ .

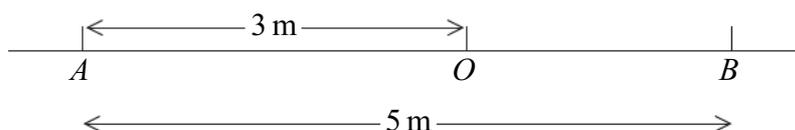
- (a) Show that  $v^2 = u^2 - 4ag$ . (2 marks)
- (b) The ratio of the tensions in the string when the bead is at the two points  $A$  and  $B$  is  $2:5$ .
- (i) Find  $u$  in terms of  $g$  and  $a$ . (7 marks)
- (ii) Find the ratio  $u:v$ . (2 marks)

Turn over ►

- 8 An elastic string has one end attached to a point  $O$  fixed on a rough horizontal surface. The other end of the string is attached to a particle of mass 2 kg. The elastic string has natural length 0.8 metres and modulus of elasticity 32 newtons.

The particle is pulled so that it is at the point  $A$ , on the surface, 3 metres from the point  $O$ .

- (a) Calculate the elastic potential energy when the particle is at the point  $A$ . (3 marks)
- (b) The particle is released from rest at the point  $A$  and moves in a straight line towards  $O$ . The particle is next at rest at the point  $B$ . The distance  $AB$  is 5 metres.



Find the frictional force acting on the particle as it moves along the surface.

(6 marks)

- (c) Show that the particle does not remain at rest at the point  $B$ . (2 marks)
- (d) The particle next comes to rest at a point  $C$  with the string slack.

Find the distance  $BC$ .

(2 marks)

- (e) Hence, or otherwise, find the total distance travelled by the particle after it is released from the point  $A$ . (1 mark)